

Find the asymptotes of the function and sketch the graph.

1. $f(x) = \frac{x+1}{x-4}$

V.A. $\rightarrow x=4$
 H.A. $\rightarrow y=1$
 y-int $(0, -1/4)$
 x-int $(-1, 0)$

2. $f(x) = \frac{x+6}{x^2-9}$

V.A. $\rightarrow x=3$ $x=-3$
 H.A. $\rightarrow y=0$
 y-int $(0, 2/3)$
 x-int $(-6, 0)$

3. $f(x) = \frac{x-3}{x^2+x-12} = \frac{x-3}{(x+4)(x-3)}$

V.A. $\rightarrow x=-4$ HOLE @ $(3, 1/4)$
 H.A. $\rightarrow y=0$
 y-int $(0, 1/4)$
 x-int NONE (3 is not in domain)

4. $f(x) = \frac{x-4}{x^2-x-6} = \frac{x-4}{(x-3)(x+2)}$

V.A. $\rightarrow x=3$ $x=-2$
 H.A. $\rightarrow y=0$
 y-int $(0, 2/3)$
 x-int $(4, 0)$

5. $f(x) = \frac{x^2-4x-21}{x^2-9} = \frac{(x-7)(x+3)}{(x-3)(x+3)}$

V.A. $\rightarrow x=3$
 H.A. $\rightarrow y=1$
 y-int $(0, 1/3)$
 x-int $(7, 0)$

6. $f(x) = \frac{1-x^2}{x^2-4x-5} = \frac{(1-x)(1+x)}{(x-5)(x+1)}$

V.A. $\rightarrow x=5$
 H.A. $\rightarrow y=-1$
 y-int $(0, -1/5)$
 x-int $(1, 0)$

7. $f(x) = \frac{(2x-1)^2}{(1-3x)^2}$

V.A. $\rightarrow x=1/3$
 H.A. $\rightarrow y=4/9$
 y-int $(0, 1)$
 x-int $(1/2, 0)$

8. $f(x) = \frac{4x+1}{6+x^2}$

V.A. \rightarrow None
 H.A. $\rightarrow y=0$
 y-int $(0, 1/6)$
 x-int $(-1/4, 0)$

* 9. $f(x) = \frac{5+x}{2x^3+8x^2+x-2}$

Use calc to find domain restrictions

V.A. $\rightarrow x=-3.8$ $x=-.6$ $x=.4$
 H.A. $\rightarrow y=0$
 y-int $(0, -5/2)$
 x-int $(-5, 0)$

10. $f(x) = \frac{2x^3-x^2-18x+9}{3x^3+3x^2-36x} = \frac{(x+3)(x-3)(2x-1)}{3x(x+4)(x-3)}$

V.A. $\rightarrow x=0$ $x=-4$ HOLE @ $(3, 1/4)$
 H.A. $\rightarrow y=2/3$
 y-int \rightarrow None
 x-int $\rightarrow (-3, 0)$ $(1/2, 0)$

11. $f(x) = \frac{x^2+3x-4}{x-2} = \frac{(x+4)(x-1)}{x-2}$

V.A. $\rightarrow x=2$
 H.A. \rightarrow None
 slant $\rightarrow y=x+5$
 y-int $(0, 2)$
 x-int $(-4, 0)$ $(1, 0)$

12. $f(x) = \frac{2x^2+9x-5}{x+3} = \frac{(2x-1)(x+5)}{x+3}$

V.A. $\rightarrow x=-3$
 H.A. \rightarrow None
 slant $\rightarrow y=2x+3$
 y-int $(0, -5/3)$
 x-int $(1/2, 0)$ $(-5, 0)$

13. $f(x) = \frac{5x^2-8x-4}{5x} = \frac{(5x+2)(x-2)}{5x}$

V.A. $\rightarrow x=0$
 H.A. \rightarrow None
 slant $\rightarrow y=x-8/5$
 y-int \rightarrow None
 x-int $(-2/5, 0)$ $(2, 0)$

14. $f(x) = \frac{x^3-5x^2-4x+20}{x^2-1} = \frac{(x+2)(x-2)(x-5)}{(x+1)(x-1)}$

V.A. $\rightarrow x=-1$ $x=1$
 H.A. \rightarrow None
 slant $\rightarrow y=x-5$
 y-int $(0, -20)$
 x-int $(-2, 0)$ $(2, 0)$ $(5, 0)$

* USE CALC FOR X-INT

15. $f(x) = \frac{x^3 - 9x^2 + 3x - 12}{x^2 - x - 6}$

V.A. $\rightarrow x=3 \quad x=-2$

H.A. \rightarrow None

Slant $\rightarrow y=x-8$

Y-int $(0, 2)$

X-int $(8.81, 0)$

$$\begin{array}{r} x-8 \\ x^2-x-6 \overline{) x^3-9x^2+3x-12} \\ \underline{-(x^3-x^2-6x)} \\ -8x^2+9x-12 \\ \underline{-(8x^2+8x+48)} \\ x-60 \end{array}$$

16. $f(x) = \frac{x^4 - 3x^3 + x^2 - 4}{x^3 + 1} = \frac{*calc}{(x+1)(x^2+x+1)}$

V.A. $\rightarrow x=-1$

H.A. \rightarrow None

Slant $\rightarrow y=x-3$

Y-int $\rightarrow (0, -4)$

X-int $\rightarrow (-.928, 0) (2.82, 0)$

$$\begin{array}{r} x-3 \\ x^3+0x^2+0x+1 \overline{) x^4-3x^3+x^2+0x-4} \\ \underline{-(x^4)} \\ -3x^3+x^2-4x-4 \\ \underline{-(-3x^3+x^2-4x-3)} \\ -1 \end{array}$$

17. $f(x) = \frac{2x^4 - 4x^3 + x - 9}{1-x^4} = \frac{*calc}{(1-x)(1+x)^2}$

V.A. $\rightarrow x=1 \quad x=-1$

H.A. $\rightarrow y=-2$

Y-int $= (0, -9)$

X-int $= (-1.17, 0) (2.28, 0)$

18. $f(x) = \frac{x^4 + 3x^3 - 5x^2 - 4}{x^3 - x^2} = \frac{*calc}{x^2(x-1)}$

V.A. $\rightarrow x=0 \quad x=1$

H.A. \rightarrow None

Slant $\rightarrow y=x+4$

Y-int \rightarrow None

X-int $\rightarrow (1.5, 0) (-4.23, 0)$

$$\begin{array}{r} x+4 \\ x^3-x^2 \overline{) x^4+3x^3-5x^2-4} \\ \underline{-(x^4-x^3)} \\ 4x^3-5x^2-4 \end{array}$$

19. $f(x) = \frac{5x^4 - x^2 + 3x - 4}{x^3 + 2x^2} = \frac{*calc}{x^2(x+2)}$

V.A. $\rightarrow x=0 \quad x=-2$

H.A. \rightarrow None

Slant $\rightarrow y=5x-10$

Y-int \rightarrow None

X-int $\rightarrow (-1.15, 0) (.816, 0)$

$$\begin{array}{r} 5x-10 \\ x^3+2x^2 \overline{) 5x^4-0x^3-x^2+3x-4} \\ \underline{-(5x^4+10x^3)} \\ -10x^3-x^2+3x-4 \\ \underline{-(-10x^3-x^2+3x-4)} \\ 0 \end{array}$$

20. $f(x) = \frac{3x^4 + 2x^3 - 5}{x^3 - 4x^2} = \frac{*calc}{x^2(x-4)}$

V.A. $\rightarrow x=0 \quad x=4$

H.A. \rightarrow None

Slant $\rightarrow y=3x+14$

Y-int \rightarrow None

X-int $\rightarrow (1, 0) (-1.35, 0)$

$$\begin{array}{r} 3x+14 \\ x^3-4x^2 \overline{) 3x^4+2x^3+0x^2-5} \\ \underline{-(3x^4-12x^3)} \\ 14x^3+0x^2-5 \\ \underline{-(14x^3-56x^2)} \\ 56x^2-5 \end{array}$$

$$\begin{array}{r} 1 \mid 3 \quad 2 \quad 0 \quad 0 \quad -5 \\ \underline{3 \quad 5 \quad 5 \quad 5} \\ 3 \quad 5 \quad 5 \quad 5 \quad 0 \\ 3x^3 + 5x^2 + 5x + 5 \end{array}$$