

Solving Polynomial and Other Equations

Solve each equation. $\frac{1}{3} + 26(\frac{1}{3})$

1. $3c = 9 - 26c^{\frac{1}{2}}$

$3c + 26c^{\frac{1}{2}} - 9 = 0$

$(3c^{\frac{1}{2}} - 1)(c^{\frac{1}{2}} + 9) = 0$

$3c^{\frac{1}{2}} = 1 \quad c^{\frac{1}{2}} = -9$

$c^{\frac{1}{2}} = \frac{1}{3}$

$c = \frac{1}{9}$

$c = 81$ ~~extraneous~~

2. $16(a+5)^2 - 5 = 20$

$(a+5)^2 = \frac{25}{16}$

$a+5 = \pm \frac{5}{4}$

$a = -5 \pm \frac{5}{4}$

$a = -6\frac{1}{4}, -3\frac{3}{4}$

$-\frac{25}{4}, -\frac{15}{4}$

3. $\sqrt{2k+7} - \sqrt{k+3} = 5$

$(\sqrt{2k+7})^2 = (5 + \sqrt{k+3})^2$

$2k+7 = 25 + 10\sqrt{k+3} + k+3$

$k-21 = 10\sqrt{k+3}$

$k^2 - 42k + 441 = 100k + 300$

$k^2 - 142k + 141 = 0$

$(k-141)(k-1) = 0$ $k=141$ ~~extraneous~~

5. $w^4 - 35w^2 + 216 = 0$

$(w^2 - 6)(w^2 - 36) = 0$

$(w^2 - 6)(w^2 - 36) = 0$

$w = \pm\sqrt{6} \quad w = \pm 6$

4. $\sqrt{3m-6} - \sqrt{m^2-2m} = 0$

$3m-6 = m^2-2m$

$0 = m^2 - 5m + 6$

$0 = (m-2)(m-3)$

$m = 2, 3$

$a = (x+3)^{\frac{1}{4}}$
 $a^2 - 4a + 4 = 0$

6. $(x+3)^{\frac{1}{2}} - 4(x+3)^{\frac{1}{4}} = -4$

$[(x+3)^{\frac{1}{4}} - 2][(x+3)^{\frac{1}{4}} + 2] = 0$

$(x+3)^{\frac{1}{4}} = 2$

$x+3 = 16$

$x = 13$

7. $4x^3(2x-1)^{\frac{3}{2}} - 8x^2(2x-1)^{\frac{1}{2}} = 0$

$4x^2(2x-1)^{\frac{1}{2}} [x(2x-1) - 2] = 0$

$4x^2(2x-1)^{\frac{1}{2}} (2x^2 - x - 2) = 0$

$x = 0, \frac{1}{2}, \frac{1 \pm \sqrt{17}}{4}$

$\frac{1 \pm \sqrt{1+4(4)}}{4}$

8. $(c^2+5)^2 - 8(c^2+5) - 48 = 0$

$[(c^2+5) - 12][(c^2+5) + 4] = 0$

$(c^2-7)(c^2+9) = 0$

$c = \pm\sqrt{7}, \pm 3i$

$$9. 14y(2 + \frac{y}{2}) = y(y-1) - 20$$

$$28y + 7y^2 = y^2 - y - 20$$

$$6y^2 + 29y + 20 = 0$$

$$(6y + 5)(y + 4) = 0$$

$$6y = -5 \quad y = -4$$

$$y = -\frac{5}{6}, -4$$

$$10. 3x^5 - 3x^3 - 36x = 0$$

$$3x(x^4 - x^2 - 12) = 0$$

$$3x(x^2 - 4)(x^2 + 3) = 0$$

$$x = 0, \pm 2, \pm i\sqrt{3}$$

$$\frac{2 \pm \sqrt{4 - 4(4)}}{8}$$

$$\frac{2 \pm \sqrt{-12}}{8} = \frac{2 \pm 2\sqrt{3}i}{8}$$

$$11) (8y^3 + 1)(y - 5) = (2y + 1)(4y^2 - 2y + 1)(y - 5) = 0$$

$$(8y^4 - 40y^3 + y - 5)$$

$$-\frac{1}{2}, 5, \frac{1}{4} \pm \frac{\sqrt{3}}{4}i$$